# **MATH 504**

# Advanced Algebra

(2018 Fall Semester)

## by Ayberk Zeytin

Prerequisites: I strongly advise you to keep your undergraduate notes on abstract algebra nearby.

Credits: (3-0)3 / 7 ECTS

Outline: This will be a standard graduate algebra course. It will have basically two parts

- ► Group Theory
- ▶ Ring Theory

The first part is expected to take about 7 weeks and the second will last for the remaining 7 weeks. We will review standard concepts (rather fast) to make time for the new ones. You will (hopefully) have 7 exercise sheets - one sheet every two weeks is the plan. These exercise sheets are aimed at providing you with a working knowledge and can be viewed as a preparation for the exams. Below is a tentative outline:

- 1 week Groups, subgroups, normal subgroups and many examples
- 1 week quotient groups, isomorphism theorems,
- 1 week direct products, free groups,
- 1 week group actions and Sylow theorems
- 1 week nilpotent and solvable groups
- 1 week Rings, ring homomorphisms, examples (polynomial rings and formal power series rings)
- 1 week ideals and rings of quotients, isomorphism theorems
- 1 week factorization in commutative rings, principal ideal domains, Euclidean domains, unique factorization domains.
- 1 week Modules, homomorphisms,
- 1 week exact sequences, free modules, modules over a PID
- 4 weeks Fields, field extensions, the fundamental theorem of Galois theory

Course web page: http://math.gsu.edu.tr/azeytin/this-semester.html

### Bibliography:

- Dummit, S., Foote, Abstract Algebra
- Grove, L. C., Algebra
- Hungerford, T. W., Algebra
- Jacobson, N., Basic Algebra
- Lang, S., Algebra

Programme: Monday 10h00 - 13h00 @ Seminer Odası 2

### Evaluation:

• 2 MT: % 60

• Final: % 40